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In a real Hilbert space H we consider the following singularly perturbed Cauchy problem $\{\epsilon u'' + \epsilon \delta^{(t) + \delta} u' - \epsilon \delta^{(t) + A} u + B(u_{\epsilon \delta}(t)) = f(t), t \in (0, T), u_{\epsilon \delta}(0) = u_0, u'_{\epsilon \delta}(0) = u_1\}$, where $u_0, u_1 \in H, f: [0, T] \mapsto H, \epsilon, \delta$ are two small parameters, A is a linear self-adjoint operator and B is a nonlinear $A^{1/2}$ Lipschitzian operator. We study the behavior of solutions $u_{\epsilon \delta}$ in two different cases: $\epsilon \rightarrow 0$ and $\delta \geq \delta_0 > 0; \epsilon \rightarrow 0$ and $\delta \rightarrow 0$, relative to solution to the corresponding unperturbed problem. We obtain some a priori estimates of solutions to the perturbed problem, which are uniform with respect to parameters, and a relationship between solutions to both problems. We establish that the solution to the unperturbed problem has a singular behavior, relative to the parameters, in the neighbourhood of $t = 0$.